

Exercise 01.

The response in time $y(t)$ of some linear dynamical system subjected to some input $w(t)$ is given by the sum of the force-free response $y_u(t)$ and the forced response $y_f(t)$. That is,

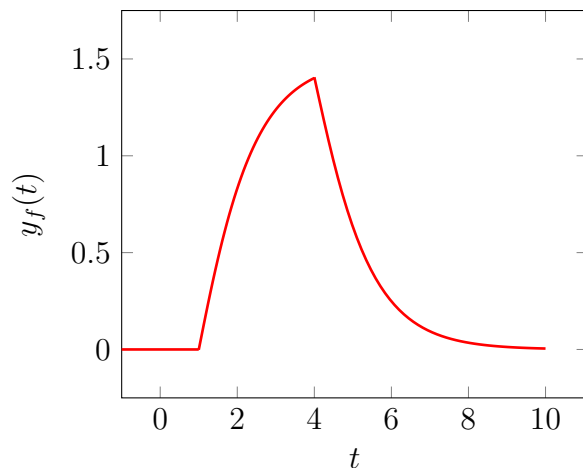
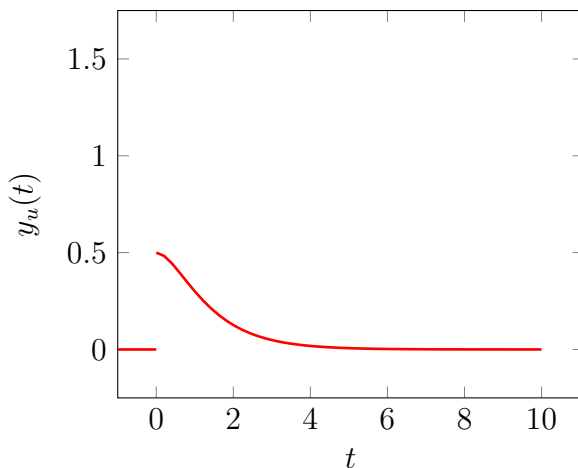
$$y(t) = y_u(t) + y_f(t).$$

Let $y_u(t)$ and $y_f(t)$ have the following expressions

$$y_u(t) = \begin{cases} 0, & t < 0 \\ e^{-t} - 0.5e^{-2t}, & t \geq 0 \end{cases};$$

$$y_f(t) = \begin{cases} 0, & t \in (-\infty, 1) \\ 1.5 - 5.44e^{-t} + 3.69e^{-2t}, & t \in [1, 4) \\ 104e^{-t} - 1487e^{-2t} & t \in [4, \infty) \end{cases}.$$

- Q1** Write two Python functions that given an input argument $t \in (-\infty, \infty)$ computes and returns the function values $y_u(t)$ and $y_f(t)$.
- Q2** Include your functions into a program and use them to compute $y_u(t)$, $y_f(t)$ and $y(t)$ when $t \in \{-1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$. Use lists to store computed function values.



Solution:

```
1 #####
2 def yu(t): #
3     if t < 0: #
4         u = 0 #
5     else: #
6         u = 0.2 + 1.91*exp(-t)*cos(2*t-1.68) #
7     return u #
8 #####
9
10 #####
11 def yf(t): #
12     if t < 1: #
13         yf = 0 #
14     elif (t >= 1) and (t < 4): #
15         yf = 1.5 - 5.44*exp(-t) + 3.69*exp(-2*t) #
16     elif t >=4: #
17         yf = 104*exp(-t) - 1487*exp(-2*t) #
18     return yf #
19 #####
20
21 from math import exp, cos
22
23 T = [-1,0.1,2.3,4,5,6,7,8,9]
24
25 lT = len(T)
26
27 yU = [0]*lT
28 yF = [0]*lT
29 y = [0]*lT
30
31 for it in range(lT):
32     yU[it] = yu(T[it]) # YU = [yu(T[it]) for it in range(lT)]
33     yF[it] = yf(T[it]) # YF = [yf(T[it]) for it in range(lT)]
34     y[it] = yU[it] + yF[it] # Y = [YU[it] + YF[it] for it in range(lT)]
```