

Exercise 01. Consider the linear time-invariant system in IO representation

$$\frac{d^3y(t)}{dt^3} + 6\frac{d^2y(t)}{dt^2} + 13\frac{dy(t)}{dt} = 2\frac{d^2u(t)}{dt^2} + 3u(t)$$

1. Determine the characteristic polynomial and its roots;
2. Determine the modes of the system, classify and plot them;
3. Let $t_0 = 0$, determine the force-free evolution from initial conditions

$$\begin{aligned}y(t)\Big|_{t=t_0} &= 1 \\ \frac{dy(t)}{dt}\Big|_{t=t_0} &= 1. \\ \frac{d^2y(t)}{dt^2}\Big|_{t=t_0} &= 1\end{aligned}$$

Exercise 02. Consider the linear time-invariant system in IO representation

$$2\frac{d^2y(t)}{dt^2} + 4\frac{dy(t)}{dt} + 2y(t) = 3\frac{du(t)}{dt} + u(t)$$

1. Define and determine the system's impulse evolution.