Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Stochastic algorithms

Federal University of Ceará, Fortaleza

Intro

Francesco Corona

Department of Computer Science

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content

Consider the general problem of system analysis and controller design

- We have at our disposal a wealth of knowledge
- Deterministic system and control theory
- We can investigate the system structure and modes of response
- We can design compensators that alter these characteristics
- We can design controllers that provide appropriate inputs
 - To generate desired system responses

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content

Stochastic algorithms

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content (cont.)

Why do we need to go beyond these results?

• Why stochastic models?

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content (cont.)

To observe the actual system behaviour, we construct measurement devices

• They output data signals, proportional to variables of interest

These signals and the known inputs are the only available information

• Information discernible about the system

If we design a controller, these signals are the only available inputs

• Direct inputs to the controller

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content (cont.)

We cannot assume perfect knowledge of all quantities or perfect control

We must develop a system model that accounts for uncertainties

- → How to optimally estimate the quantities of interest?
- → How to optimally control the system to perform?

How to evaluate the performance of these estimates and control?

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

General content (cont.)

No mathematical system model is considered perfect

- Only dominant/critical modes are modelled
- Computationally feasible (light)

Systems are not only driven by our control inputs

- Disturbances that we cannot control
- Disturbances that we cannot model

Sensors are not perfect nor they are complete

- Not all interesting information
- · No exact reading and noise
- Own system dynamics

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

General content (cont.)

The course is an introduction to modelling of dynamic processes

- Deterministic and stochastic state-space models
- Deterministic and random Markov functions

We overview of dynamic system analysis and probability theory

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Deterministic Markov functions

Deterministic Markov functions

General content

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Deterministic Markov function

Deterministic Markov functions (cont.)

The analysis of state-space models only in the time-domain

→ Linear and stationary models

A general scheme to determine the state transition matrix

→ The Sylvester expansion

A general procedure to solve the analysis problem

→ The Lagrange formula

Similarity transformations and canonical forms

- → Diagonalisation
- → Jordan's form

The system modes and their interretation

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Markov functions

Deterministic Markov functions

Deterministic Markov systems/models and their classification

- Input-output and state-space representation
- \leadsto Focus on state-space models

General properties of deterministic systems

- Dynamical/Instantaneous
- Linear/Nonlinear
- Stationary/Nonstationary
- Proper/improper
- With/Without delay



Stochastic Markov functions

General content

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content Deterministic Markov functions Stochastic Markov

functions Logistic

Evaluation

Stochastic Markov functions

Stochastic Markov system/models, their classification and their properties

- Continuous-time continuous-state Markov processes
- Continuous-time discrete-state Markov processes
- Discrete-time discrete-state Markov processes

Main focus on discrete-time discrete-state processes

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

Deterministic Markov functions Stochastic Markov functions

Logistic

Evaluation

Stochastic Markov functions (cont.)

Analysis of continuous-time discrete-state Markov processes

- General concepts and definitions
- Transition probabilities
- Transition rates

Some important distributions

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Deterministic
Markov functions
Stochastic Markov

Logistic

Evaluation

Stochastic Markov functions (cont.)

Analysis of discrete-time discrete-state Markov processes (chains)

- General concepts and definitions
- Classification of states
- Irreducibility

Some important matrices

- Fundamental matrix
- Reachability matrix
- Potential matrix

Some important distributions

- Steady-state distribution
- Stationary distribution
- Limiting distribution

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Deterministic
Markov functions
Stochastic Markov

- ----

Evaluation

Stochastic Markov functions (cont.)

Continuous-time continuous-space (general) Markov processes

- General Markov state density function
- Chapman-Kolmogorov equations
- Kramers-Moyal equations
- The Markov propagator

Time-integral and time-evolution of Markov processes

• General moment evolution equations

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Content

Markov functions

Stochastic Markov functions

Logistic

Evaluation

Stochastic Markov functions (cont.)

The continuous propagator and its characterising functions

• Time-evolution equations

Three important continuous Markov processes

- The Liouville process
- The Weiner process

The Fokker-Planck equation and the Langevin equation

Ornstein-Uhlenbeck process

L

uFC/DC SA (CK0191) 2018.1

Stochastic

Content

Deterministic
Markov functions
Stochastic Markov
functions

Logistic

Evaluation

Logistic

SIGAA doesn't know the course location

• Here, mostly

Timetable, as you have known it

- Friday afternoons
- $14:00 \rightarrow 18:00$
- SIGAA's wrong

I do not care about presence

• If you deliver

Stochastic algorithms UFC/DC SA (CK0191) 2018.1 Content Deterministic Markov functions

Logistic

Logistics

Stochastic algorithms



UFC/DC SA (CK0191) 2018.1

Content

Deterministic Markov functions Stochastic Marko functions

Logistic

Evaluation

Evaluation

Stochastic algorithms

Stochastic algorithms

UFC/DC SA (CK0191) 2018.1

Conten

Deterministic
Markov functions
Stochastic Markov
functions

Logistic

Evaluation

Evaluation

Two, maybe three, intermediate tests (AP) here in the classroom (70%)

• Train by exercising and participating

One, maybe two, home assignment/project (30%)

To pass the course you need a 5, with 7 you pass earlier (8, I am happy)

• You can have a final test (AF), if you ask